Unification-Based Query Language for Relational Knowledge Bases and Its Parallel Execution

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ABSTRACT

Relational database systems are very useful and widely accepted as the systems that handle large amounts of data efficiently. However, the expressive power of the data model is limited because of the restriction of the first normal form. This limitation prevents storage of knowledge representing data with a complicated structure to a traditional database system and prevents the realization of applications using large amounts of knowledge. The relational knowledge base (RKB) model was introduced to remove such limitations on the logic programming language. The RKB enables Prolog terms to be stored and manipulated within the framework of the relational model.

This paper introduces a manipulation language for sets of terms stored in the RKB. This manipulation language is embedded in the logical programming language and enables it to manipulate large amounts of knowledge represented by terms. Because our manipulation language can handle terms using the unification operation, unification-based logic programming languages can incorporate functions to manipulate sets of terms stored in the RKB without operational gaps.

1 INTRODUCTION

As knowledge information processing technology advances, many knowledge-based systems, such as expert systems, will be made for practical use. The amount of knowledge and the degree of complexity of knowledge representing data used in such systems will increase according to the degree of maturation. Such knowledge will be required to be shared by knowledge-based systems on the analogy of traditional database systems.

In recent years, logic programming languages have become very popular in the design and implementation of knowledge-based systems. However, these systems are established with the premise that all knowledge is included as part of the systems in spite of the fact that they must handle large amounts of knowledge or that they have a knowledge base management system for private use. In such situations, it is necessary to establish a dedicated system which can efficiently manage and store large amounts of knowledge, that is, knowledge representing data with a complex structure, shared by several knowledge information processing systems. We call this dedicated system a knowledge base system.

Database systems are very useful and widely accepted as systems to manipulate and store large amounts of data. However, the expressive power of the data model is limited because of restrictions such as the first normal form of the relational database. This limitation prevents the use of traditional database systems as the back end of logic programming languages which use structured terms as the basic data structure. Recently, much research has been conducted towards extending the traditional data model and adding more useful semantics to it [7][8][14]. For the relational data model in particular, many extensions have been made because of its formally definable semantics.

We are researching a knowledge base system which can be accessed from knowledge information processing systems based on the logic programming language in Japan’s Fifth Generation Computer Project. A logic programming language can be regarded as a programming language which manipulates terms as basic data structures. It can manipulate terms with a complex structure by using a unification operation. Therefore, we intend to establish knowledge base systems that can store and manipulate large amounts of terms efficiently.

We have proposed a relational knowledge base (RKB) model as an extended relational data model which can store a set of terms to a table (relation) and manipulate terms by extended relational algebraic operations based on a unification operation [5][13]. The collection of these extended relations is called the RKB and the extended operations are collectively called retrieval by unification (RBU) operations. We have also proposed an architecture of the knowledge base machine (KBM) with processing elements and a multiport page-memory. On this KBM, each RBU operation is executed in parallel for the
fast retrieval of RKB.

The major contribution of this paper is to show how to embed a manipulation language for the RKB in logic programming languages. Introducing the unification operation as a basic operation, the manipulation language is naturally embedded in a logic programming language. This embedding will provide a convenient environment for logic programming languages when a large amount of knowledge is required. This paper introduces a query language in the form of predicates of the logic programming language, which can define the retrieval and updating of sets of terms. This paper also explains how to execute our manipulation language in parallel on our KBM.

The remainder of this paper describes the relational knowledge base model, manipulation language for RKB and its parallel execution. Section 2 reviews the relational knowledge base model. Section 3 defines queries for the relational knowledge base. Section 4 describes our manipulation language for term relations. Section 5 briefly describes the architecture of our KBM and the way to execute our manipulation language in parallel on this KBM. Lastly, Section 6 is a discussion and a summary of this paper.

2 OVERVIEW OF THE RELATIONAL KNOWLEDGE BASE MODEL

This section overviews the relational knowledge base model. This model allows us to define terms as attribute values of the relational scheme and to manipulate these terms by unification operations. Because items stored to each relation are terms, instances of the relational scheme are called term relations.

A relational knowledge base is a collection of term relations. An n-attribute term relation is defined as a relation whose domain of each attribute is a set of terms. Here, we define terms as:

1. A variable is a term.
2. A constant is a term.
3. If f is an n-ary function symbol and t₁, t₂, ..., tₙ are terms, then f(t₁, t₂, ..., tₙ) is a term.

This definition of terms is the same as logic programming languages such as Prolog. Expressing a set of terms, \( K_n \), an n-attribute term relation is defined as a subset of the Cartesian product of sets of terms, \( K_1 \times K_2 \times \cdots \times K_n \) [5][13]. Assuming that \( T \) is an n-attribute term relation, \( T \) is defined as:

\[
T \subseteq K_1 \times K_2 \times \cdots \times K_n.
\]

In the process of extending the relational data model to the relational knowledge base model, operations of conventional relational algebra, such as join, projection, and restriction, are extended to operations based on unification. We call these extended operations RBU operations. The extension was made by enhancing the equality check between constants to unification operation between terms. The unification-join and unification-restriction operations are defined as RBU operations [5][13].

Let us consider a simple knowledge base which will be used to illustrate the relational knowledge base model. In the following, we express a tuple of an n-attribute term relation, \( r \), as:

\[
r(x_1, x_2, \cdots, x_n)
\]

where each \( x_i \) stands for a term defined above. Each tuple with the same relation name and the same number of attributes is stored to the relation with the same relation name. Moreover, we assume the conventions of DBC-10 Prolog, such that any word starting with either a capital letter or _ denotes variables, and other words denote constants.

Allowing terms as attribute values, many expressions become possible. The following is a simple bicycle relation which expresses a module-submodule relation among modules constructing bicycles. Although there are several submodules for one module, we can express that relation in just one tuple using a list structure.

Example 1 Module-submodule relation of bicycles

assembly(bike,[frame,wheel]).
assembly(frame,[front_fork,diamond_frame]).
assembly(wheel,[tire,rim,spokes,hub]).

For example, the first tuple expresses the fact that the bike module has wheel and frame as submodules.

Introducing n-ary functors, we can add more attributes to each item. For example, we can distinguish colors among modules by introducing a color attribute for each item.

Example 2 More complex expressions using functors

assembly(bike(red),[frame(red),wheel]).
assembly(bike(yellow),[frame(yellow),wheel]).
assembly(frame(red),
fronct_fork(red),diamond_frame(red))).
assembly(frame(yellow),
front_fork(yellow),diamond_frame(yellow))).
assembly(wheel,[tire,rim,spokes,hub]).

This shows, for example, that a red bike has a red frame and a red frame is composed of a red front_fork and a red diamond_frame.

By introducing variables, we can express the property inheritance between a module and its submodule. For example, the following tuple expresses the fact that front_fork and diamond_frame have the same color as frame.
Example 3  Expression of property inheritance using variables

\text{assembly}(\text{bikes(red)}, \{\text{frame(red)}, \text{wheel}\}).
\text{assembly}(\text{bikes(yellow)}, \{\text{frame(yellow)}, \text{wheel}\}).
\text{assembly}(\text{frame}(X),
  \{\text{front.fork}(X), \text{diamond.frame}(X)\}).
\text{assembly}(\text{wheel}, \{\text{tire}, \text{rim}, \text{spokes}, \text{hub}\}).

As stated above, relational algebraic operations are extended to RBU operations. The RBU operations allow the unification operation to be used between terms as conditions of relational algebraic operations. In the following, we use $\sigma$ to denote the unification operation as a condition, and use many symbols defined in [12] to denote relational algebraic operations, i.e., $\sigma$, $\cap$, and $\pi$ for restriction, join, and projection, respectively.

Using the unification-restriction operation, we can restrict tuples whose first attribute can be unified with bike(X) from the assembly relation of Example 3. Supposing that the results of this restriction are stored into the new two-attribute relation, result(X, X), this operation can be expressed as follows.

\text{result1} = \sigma_{A_1, \text{wheel(X)}} \text{assembly}(A_1, A_2)

Example 4 is the result of this operation.

Example 4  Result of the unification-restriction

\text{result1}(\text{bikes(red)}, \{\text{frame(red)}, \text{wheel}\}).
\text{result1}(\text{bikes(yellow)}, \{\text{frame(yellow)}, \text{wheel}\}).

We can make a list of parts that are necessary to make bike(red) and bike(yellow) from assembly of Example 3 and the result1 relation. First, to extract submodules one by one from the list of the second attribute of the assembly relation, we must introduce a special relation, template, which has only one tuple, such as:

template(X, Y, \{X\}, Y).

and make the following unification-join operation between the template relation and assembly relation.

temp =
\pi_{A_1, A_2}(\text{template}(A_1, A_2, A_3) \cap A_3 \cap B_1 \text{assembly}(B_1, B_2))

We can obtain the temp relation below as a result.

temp(frame(red), \{wheel\}).
temp(frame(yellow), \{wheel\}).
temp(front.fork(X), \{diamond.frame(X)\}).
temp(tire, \{rim, spokes, hub\}).

Then, making the unification-join between the temp relation and the assembly relation, we can obtain the relation of Example 5.

result2 =
\pi_{B_1, B_2}(temp(A_1, A_2) \cap \text{assembly}(B_1, B_2))

The frame(X) in the first attribute of the assembly relation is unified with \text{frame(red)} and \text{frame(yellow)} in the first attribute of the temp relation, and the binding to variable X is propagated to terms in the remaining attribute.

Example 5  Result of the unification-join

result2(frame(red),
  \{\text{front.fork(red)}, \text{diamond.frame(red)}\}).
result2(frame(yellow),
  \{\text{front.fork(yellow)}, \text{diamond.frame(yellow)}\}).

Although other operations, such as aggregate functions, are not described above, the relational knowledge base model includes them with the same operational semantics defined in the relational data model.

3 QUERIES TO THE RKB

This section considers how to access term relations from a logic programming language. A logic programming language can be regarded as a programming language that manipulates terms as a basic data structure. The RKB enables direct storage and manipulation of terms. These functions are effective in managing and storing large amounts of knowledge represented by terms.

Term relations are manipulated by the relational algebraic operations in the previous section. Those relational algebraic operations are procedural operations. Because a logic programming language is rather declarative, it is necessary to make manipulation language declarative so that it can be embedded in the logic programming language without operational gaps.

3.1 Relational Calculus for the RKB

For the relational data model, we already have a declarative manipulation language, called relational calculus, which is based on predicate calculus. Because predicate calculus is also a logic programming language base, it is desirable to establish a manipulation language for the RKB based on relational calculus.

This section gives an informal definition of the manipulation language for the RKB, based on relational calculus. It can be considered as an implementation of domain relational calculus for term relations. Referencing the definition of domain relational calculus in [12], we extend it for the term relations. The extension is made by extending the domain of each calculus to the set of terms and operations defined between constants to the unification operation between terms.

Expressions in domain relational calculus for the term relations are of the form:

\{t_1, t_2, \ldots, t_k \mid \psi(x_1, x_2, \ldots, x_l)\},

where each $t_i$ ($1 \leq i \leq k$) and $x_j$ ($1 \leq j \leq l$) is a term and $\psi$ is a formula built from terms and atomic formulas.
defined below. Each \( t_i \) can include the same variables used in each \( x_j \) so that when variables in each \( x_j \) are instantiated in the evaluation of \( \psi \), bindings are propagated to the corresponding variables in each \( t_i \). Atomic formulas forming \( \psi \) are defined as follows:

\[
\rho(x_1, x_2, \ldots, x_l): \text{where } \rho \text{ is the relation name of an } l\text{-}
\]

attribute term relation and every \( x_i \) is a term.

\[
\exists \theta \text{xy : where } x \text{ and } y \text{ are terms and } \theta \text{ is an operator}
\]

defined between terms.

In the definition of domain relational calculus for the relational data model, each \( x_j \) must be a constant or a variable, and \( \rho(x_1, x_2, \ldots, x_l) \) merely asserts that the value of each \( x_j \) variable must be selected so that \( x_1, x_2, \ldots, x_l \) is in relation \( \rho \). However, we must extend this definition so that it can manipulate sets of terms.

The first type of atomic formula asserts the following. Suppose that \( <y_1, y_2, \ldots, y_l> \) denotes an arbitrary tuple of relation \( \rho \), the value of each \( x_j \) (1 \( \leq \) j \( \leq \) l) must be \( x_j \) such that \( \rho(x_1, x_2, \ldots, x_l) \) is the result of unification between \( \rho(x_1, x_2, \ldots, x_l) \) and \( \rho(y_1, y_2, \ldots, y_l) \). That is, there is a most general unifier, \( \beta \), between \( \rho(x_1, x_2, \ldots, x_l) \) and \( \rho(y_1, y_2, \ldots, y_l) \), such that

\[
\rho(x_1, x_2, \ldots, x_l) = \rho(x_1, x_2, \ldots, x_l) \beta = \rho(y_1, y_2, \ldots, y_l) \beta.
\]

For example, supposing that \( X \) and \( Y \) are variables, we can select all tuples from the assembly relation of Example 3 using the formula of \( \text{assembly}(X, Y) \). Using the formula \( \text{assembly}(\text{bike}(X), Y) \), we can select the same tuples as Example 4.

The second type of atomic formula, \( \exists \theta \text{xy} \), asserts that \( x \) and \( y \) must be terms that make \( \exists \theta \) true. \( \theta \) is also extended from an arithmetic relational operator to the operator defined between terms. The next section introduces various kinds of relational operators between terms.

Atomic formulas may be combined by means of logical operations such as \( \lor \), \( \land \), and \( \neg \). We define formula \( \psi \) recursively as follows:

1. Every atomic formula is a formula.
2. If \( \psi_1 \) and \( \psi_2 \) are formulas, then \( \psi_1 \lor \psi_2 \), \( \psi_1 \land \psi_2 \), and \( \neg \psi_1 \) are formulas. These formulas assert respectively that \( \psi_1 \) or \( \psi_2 \), or both are true", \( \psi_1 \) and \( \psi_2 \) are both true", and \( \psi_1 \) is not true".

3.2 Relational Operations between Terms

For the relational data model, arithmetic relational operators are sufficient to compare constants. However, these arithmetic operators cannot handle structured data types such as terms. Therefore, it is necessary to add other relational operators which are defined between terms for the RKB. This section introduces relational operations between terms. These operations are based on unification, unifiability, arithmetic comparison, and generality between terms.

In the following, it is assumed that \( x \) and \( y \) stand for terms. Each operator is defined as follows:

(1) Unification

Unification is one of the most necessary operation primitives to manipulate terms. We have defined three kinds of operators relating to unification.

When we want to unify two terms or extract substructures from terms, we can do it using the unification operation, which is shown by \( = \). \( x = y \) asserts that it is true when two terms are unifiable and \( x \) is unified with \( y \). For example, when the following formulas are used for the assembly relation of Example 3,

\[
\text{assembly}(X, Y) \land (X = \text{bike}(A))
\]

we can select the first two tuples, whose first attribute's value is \( \text{bike}(A) \) of the assembly relation, and obtain \( \{\text{red}, \text{yellow}\} \) as a set of bindings to variable \( X \).

Sometimes, it is necessary only to test whether two terms can be unified or not without applying their substitutions. We call this a unify-check operation and assign the \( <> \) symbol to it. For example, when the above formula is:

\[
\text{assembly}(X, Y) \land (X <> \text{bike}(A))
\]

it merely selects the first two tuples, and cannot obtain any bindings for the variable, \( X \).

(2) Generality

When we want to know if several terms have the same structure or if several terms may have the same meaning in our semantic definition for terms, neither the unification nor the unify check operation can be used. To enable this, the generality of terms should be compared. The generality of terms is defined as follows.

Generality: Between terms \( t \) and \( u \), \( t \) is defined as more general than \( u \) if and only if there is a substitution, \( \beta \), such that \( t \beta = u \).

According to the above definition, \( t(X, Y) \) is more general than \( t(3, 2) \). This is shown using \( <> \):

\[
t(X, Y) <> t(3, 2).
\]

When one term is more general than the other and vice versa, the generality of these terms is regarded as equal. For example, \( t(X, Y) \) and \( t(A, B) \) is such a case. This is denoted \( <<< \), as follows.
According to the above definition, if the generality of two terms is equal, they can be made literally identical by appropriately renaming the variables of one term. Note that there are many cases when the generality order is not applicable. For example, we cannot decide the generality between \( r(X, S) \) and \( r(\Phi, Y) \).

### 3.3 Query Expressions in the Form of Calculus

As stated in the preceding sections, queries for the RKB are expressed as a combination of two kinds of atomic formulas. This section gives some query expressions using atomic formulas defined in the preceding sections by examples. Suppose that each \( t_i \) and \( \tau_j \) is a term, and a calculus expression is an expression of the form:

\[
\langle t_1, t_2, \ldots, t_k \rangle\ 
|\psi(s_1, s_2, \ldots, s_l)\rangle
\]

The unification-join between relations \( r(X, Y) \) and \( t(Z, W) \) is expressed as:

\[
\langle X, Y, W \rangle \land \langle r(X, Y) \land t(Z, W)\rangle
\]

Attributes used to join are designated by the same variable name. In this case, \( x \) and \( t \) are joined on the second attribute of \( z \) and the first attribute of \( t \). The bindings to each variable of one predicate are propagated to variables with the same variable name in other predicates, the same as the execution of Prolog clauses. We can rewrite this formula using the unification operator, \( = \), as follows:

\[
\langle X, Y, W \rangle \land \langle r(X, Y) \land t(Z, W) \land (Y = Z)\rangle
\]

Moreover, equijoin can be asserted by the literally-equal operator, \( = \), as follows.

\[
\langle X, Y, W \rangle \land \langle r(X, Y) \land t(Z, W) \land (Y == Z)\rangle
\]

A restriction operation which obtains tuples in result 1 of Example 4 from result of Example 3 is expressed as:

\[
\langle bike(X), Y \rangle \land \langle assembly(bike(X), Y)\rangle
\]

Lastly, unification-join and projection between result 1 and assembly to obtain result 2 of Example 5 is expressed as follows:

\[
\langle Y, Z \rangle \land \langle result(X, Y) \land assembly(Y, Z)\rangle
\]
the retrieve predicate. They are used only for specifying where values that satisfy the conditions of Query are placed in the resultant relation.

The remaining three predicates are retrieval operations to which aggregate functions are added. Each predicate corresponds to sorting, to making unique, and to grouping tuples of the resultant relation. Attribute specifies attribute variables used in Relation in the form of a list. Sorting and grouping are performed according to the values of attributes designated in this list. EqOp and EqOpList denote relational operations that are used to compare values to execute each aggregate function.

(2) Tuple reference

Format:
get(Tuple)
getAsList(List,Number,Relation)

Meaning:
As stated above, the retrieve predicate returns no binding values with respect to the tuples in the resultant relation. Therefore, we need a predicate to reference values of each tuple in the term relation. We have two kinds of predicate to refer the values of each tuple. One refers tuples one by one, and the other refers all tuples of the designated term relation at once.

The get(Tuple) predicate is the first kind of predicate. Tuple specifies the relation name and its attribute. For example, we can specify assembly(frame(X),1) as Tuple for Example 2. Tuple is unified with one of the tuples in the designated relation, and bindings that are the result of this unification will be returned. We can access all tuples in the term relation designated by Tuple using backtracking. That is, in redoing get, an alternative tuple is unified to Tuple.

The getAsList(List,Number,Relation) predicate returns the number of tuples specified by Number from the relation specified by Relation to List in the form of a Prolog list. Being different from the get predicate, this predicate returns values in the form of tuple with the relation name. For example, we can use getAsList(X,Y) for tuple-wise reference or getAsList(List,Number,Relation) for reference of the first 3 tuples for the assembly relation of Example 2.

(3) Tuple insertion

Format:
put(Tuple)
putAsList(List)

Meaning:
In the same way as tuple reference, we have two kinds of predicate for tuple insertion into the term relations. They are put(Tuple) for tuple-wise insertion and putAsList(List,Relation) for insertion of a set of tuples. The arguments, Tuple and List, play the same role as the get and getAsList predicates.

That put(Tuple) predicate inserts a tuple that is specified in Tuple argument or currently instantiates Tuple argument when it is executed. Tuple specifies the relation name and its attributes in the same way as the get predicate does. However, the attributes must be instantiated to values stored into the relation. The relation name of this tuple is used as specifications for the target relations into which the tuples are inserted. That is, target relations are decided dynamically according to the values of the Tuple argument when the predicate is executed.

For example, when we write put(assembly(bike(X), wheel(frame(X)))), the assembly(bike(X),wheel(frame(X))) tuple is inserted into the assembly relation of Example 2. Besides, suppose that variable X was bound to blue before the put predicate is executed. The assembly(bike(blue), wheel(frame(blue))) tuple will then be inserted.

The putAsList(List) predicate inserts a set of tuples stored in List in the form of the Prolog list into a relation. This predicate also uses the relation name of tuples as specification for the output relation. Each tuple must have the same relation name.

We realize not by the difference operation between term relations, that is, we express the negation of a relation in a relative complement expression. Therefore, we provide a meta-level predicate, such as dif(A,B,θ), where A and B are relations with the same attribute number and θ is a relational operator, as a Query of the retrieve predicate. dif(A,B,θ) asserts the set of tuples a in A such that, for arbitrary tuple b in B, aθb is not true if A and B have the same number of attributes. θ must be =, <>, or <=.
5 Parallel Execution of the Manipulation Language

The RKB is implemented on an experimental knowledge base machine (KBM) which is a multiprocessor system with a multiport page-memory [4][6]. We connected a PSI to this system as the host system. The manipulation language introduced in this paper is used as an interface language between the ESP and RKB [10].

This section describes how to execute the retrieve predicate in parallel on this KBM.

5.1 KBM Architecture

First, introduce hardware configuration of our KBM, which is the background for parallel executions of retrieve predicates, is introduced.

Figure 1 shows the basic hardware configuration of our KBM. The main components of the machine are processing elements (PEs) with disk systems, a multiport page-memory (MPPM), shared memory as an interconnection structure and a system control processor (SCP).

PEs can execute RBU operations directly inputting and outputting sets of terms from/to MPPM and communicate with each other through the shared memory. The MPPM plays the role of a workspace for each PE when it executes RBU operations. The SCP is a front-end processor for this KBM.

The MPPM is composed of a switching network with multiple input/ output ports and memory banks. An access unit of the MPPM is a page and each page is allocated horizontally in all memory banks so that each page can be accessed from several ports simultaneously without any access conflict [10].

Each RBU operation is decomposed into concurrently executable operations and distributed among each PE for parallel execution. The MPPM can be accessed simultaneously from each PE in parallel execution. All term relations are stored in the MPPM during execution of RBU operations.

5.2 Compilation and Parallel Execution of the Manipulation Language

The retrieve predicates are processed as shown in Figure 2. The query part is compiled into a sequence of RBU operations whose result is in the form specified in the relation part. RBU operations are decomposed into sub-operations.

Compilation is made by analysis in the form of an AND-OR tree. Each node of this AND-OR tree corresponds to a RBU operation, such as a-join, a-restriction, and projection, each of which handles at most two relations. Because each RBU operation can handle at most two relations as input relations at once, temporary relations are introduced in compilation. The root node corresponds to the resultant relation of a retrieve operation. After the AND-OR tree has been created, a sequence of RBU operations is generated from the tree. Figure 3 shows an example of an AND-OR tree.

The compiled RBU operations are executed in parallel on our KBM for fast execution. As explained above, each RBU operation is decomposed into concurrently executable sub-operations. This decomposition is made by horizontally partitioning one relation which is input to a RBU operation. Then, these decomposed sub-operations are distributed among PEs and executed concurrently. In this method for parallel execution, relations on the MPPM may be accessed simultaneously from several PEs. However, each PE can access relations without any conflict because the MPPM can provide each PE with an independent data transfer path. This decompositions are made in executing the sequence of RBU operations which is generated as the result of the above
6 CONCLUSION

This paper introduced a manipulation language for the RKB. The RKB is an extension of a relational database, which can store and manipulate sets of terms directly. The manipulation language introduced in this paper can manipulate terms using the unification operation and provides functions to access sets of terms stored in the RKB from a logic programming language. For fast retrieval, our manipulation language is executed in parallel on our KBM, which is a multiprocessor system with a large-scale shared memory.

There are approaches to integrate database systems and logic programming languages, such as deductive database systems [1][9]. Deductive database systems are discussed on the premise that large numbers of facts are stored into relational database systems. The RKB can provide fuller expressiveness power to model knowledge than the relational database. Therefore, the RKB can carry a greater part than the relational database when we integrate a logic programming language and a database system. However, our manipulation language cannot express recursive queries at present. Recursive queries are one of the most important features for realizing deduction on a knowledge base. A future research topic is to incorporate the expression of recursive queries.

As described in [11], the impedance mismatch between the relational query and a logic programming language must be taken into consideration when the method of integrating them is considered. This mismatch originates in the fact that, although the relational queries are based on set-at-a-time semantics, the logic programming language is based on tuple-at-a-time semantics. LDL [11] intends to resolve such problems by extending a logic programming language to be based on set-at-a-time semantics. We provide two special predicates, get and getList. These predicates enable the logic programming language to access not only one tuple at a time but also one set at a time. Compared to LDL, our manipulation language does not resolve the mismatch essentially. However, it enables a traditional logic programming language to access the RKB without any semantic change.

A future research topic.

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References